

Problemas resueltos de Cinemática

$$\textcircled{11} \quad t = 2 \text{ s}$$

¿h?

$$v_s = 340 \frac{\text{m}}{\text{s}}$$

$$g = 9.8 \frac{\text{m}}{\text{s}^2}$$

$$a) \quad e = \frac{1}{2} \cdot g \cdot t^2 =$$

$$= \frac{1}{2} \cdot 9.8 \cdot 2^2 = \boxed{19.6 \text{ m}}$$

$$b) \quad t_T = t_1 + t_2 = 2$$

$$e = \frac{1}{2} \cdot 9.8 \cdot t_1^2 = 49 \cdot t_1^2$$

$$e = 340 \cdot t_2$$

$$49 \cdot t_1^2 = 340 \cdot t_2$$

$$t_1 + t_2 = 2$$

$$t_2 = \frac{49 \cdot t_1^2}{340} =$$

$$= 0.144 \cdot t_1^2$$

$$t_1 + 0.144 \cdot t_1^2 = 2 \Rightarrow 0.144 \cdot t_1^2 + t_1 - 2 = 0$$

$$t_1 = \frac{-1 \pm \sqrt{1^2 + 4 \cdot 0.144 \cdot 2}}{2 \cdot 0.144} = 1.945 \text{ s}$$

$$e = 49 \cdot t_1^2 = 49 \cdot 1.945^2 = \boxed{18.55 \text{ m}}$$

(12) $d_0 = 1000 \text{ km}$

12 PM

$$v_A = 80 \frac{\text{km}}{\text{h}}$$

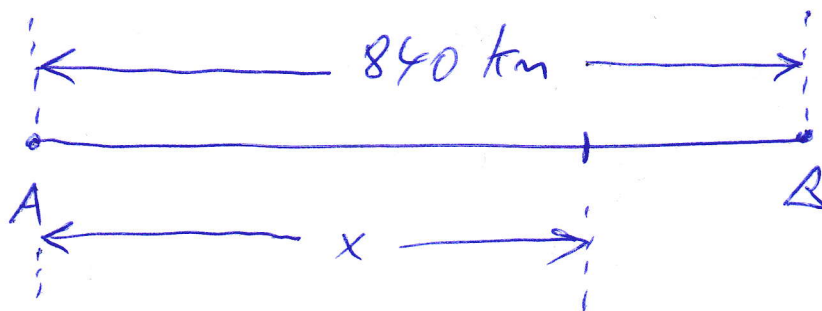
$$t = 2 \text{ h}$$

$$v_B = 100 \frac{\text{km}}{\text{h}}$$

* Distancia recorrida por A en 2 h:

$$e = v_A \cdot t = 80 \cdot 2 = 160 \text{ km}$$

$$d = d_0 - e = 1000 - 160 = 840 \text{ km}$$



$$e = v \cdot t$$

$$A: x = 80 \cdot t$$

$$B: 840 - x = 100 \cdot t$$

$$840 - 80 \cdot t = 100 \cdot t$$

$$840 = 180 \cdot t$$

$$t = \frac{840}{180} = 4\frac{2}{3} \text{ h} ; x = 80 \cdot t = 80 \cdot 4\frac{2}{3} = 374 \text{ km}$$

* Distancia recorrida por A:

$$e = 160 + 374 = \boxed{534 \text{ km}}$$

* Distancia recorrida por B:

$$e = 840 - x = 840 - 374 = \boxed{466 \text{ km}}$$

* Hora a la que se encuentran:

$$12 + 4\frac{2}{3} = 16\frac{2}{3} \text{ h}_{(2)} = \boxed{16 \text{ h } 40 \text{ min}}$$

13) $v_0 = 0$

$$v = 100 \frac{\text{km}}{\text{h}} = 27.8 \frac{\text{m}}{\text{s}}$$

$$t = 12 \text{ s}$$

a) $\hat{a}$?

b) $\hat{e}$?

$$t = 20 \text{ s}$$

c) $\hat{t}$?

$$v = 200 \frac{\text{km}}{\text{h}} = 55.6 \frac{\text{m}}{\text{s}}$$

$$t = \frac{55.6}{2.32} = \boxed{24 \text{ s}}$$

a)

$$a = \frac{\Delta v}{\Delta t} = \frac{27.8 - 0}{12 - 0} = \boxed{2.32 \frac{\text{m}}{\text{s}^2}}$$

b)

$$e = v_0 \cdot t + \frac{1}{2} \cdot a \cdot t^2 =$$

$$= 0 + \frac{1}{2} \cdot 2.32 \cdot 20^2 = \boxed{464 \text{ m}}$$

c) $v = v_0 + a \cdot t$

$$55.6 = 0 + 2.32 \cdot t$$

14) $v_0 = 60 \frac{\text{km}}{\text{h}} = 16.7 \frac{\text{m}}{\text{s}}$

$$e = 52 \text{ m}$$

$$t = 2.5 \text{ s}$$

a) $\hat{a}$?

b) $\hat{v}$?

a) $v^2 = v_0^2 + 2 \cdot a \cdot e$

$$e = v_0 \cdot t + \frac{1}{2} \cdot a \cdot t^2$$

$$52 = 16.7 \cdot 2.5 + \frac{1}{2} \cdot a \cdot 2.5^2$$

$$52 = 41.7 + 3.12 \cdot a$$

$$52 - 41.7 = 3.12 \cdot a$$

$$10.3 = 3.12 \cdot a; a = \frac{10.3}{3.12} = \boxed{3.3 \frac{\text{m}}{\text{s}^2}}$$

b) $v = v_0 + a \cdot t = 16.7 + 3.3 \cdot 2.5 =$

$$= \boxed{25 \frac{\text{m}}{\text{s}}}$$

$$(15) \quad v = 54 \frac{\text{km}}{\text{h}} = 15 \frac{\text{m}}{\text{s}}$$

$$v = 72 \frac{\text{km}}{\text{h}} = 20 \frac{\text{m}}{\text{s}}$$

$$e = 175 \text{ m}$$

$\hat{a} \text{ t?}$

$\hat{a} \text{ a?}$

$$v^2 = v_0^2 + 2 \cdot a \cdot e$$

$$20^2 = 15^2 + 2 \cdot a \cdot 175$$

$$400 = 225 + 350 \cdot a$$

$$400 - 225 = 350 \cdot a$$

$$175 = 350 \cdot a$$

$$a = \frac{175}{350} = \boxed{0.5 \frac{\text{m}}{\text{s}^2}}$$

$$v = v_0 + a \cdot t; \quad 20 = 15 + 0.5 \cdot t; \quad 20 - 15 = 0.5 \cdot t$$

$$5 = 0.5 \cdot t; \quad t = \frac{5}{0.5} = \boxed{10 \text{ s}}$$

$$(16) \quad v_2 = 25 \frac{\text{km}}{\text{h}} = 6.94 \frac{\text{m}}{\text{s}}$$

$$e = 2 \text{ km}$$

$$v_3 = 40 \frac{\text{km}}{\text{h}} = 11.1 \frac{\text{m}}{\text{s}}$$

$\hat{a} \text{ a?}$

$\hat{a} \text{ t?}$

$$v_3^2 = v_2^2 + 2 \cdot a \cdot e$$

$$11.1^2 = 6.94^2 + 2 \cdot a \cdot 2000$$

$$123 = 48.2 + 4000 \cdot a$$

$$123 - 48.2 = 4000 \cdot a$$

$$74.8 = 4000 \cdot a$$

$$a = \frac{74.8}{4000} = \boxed{0.0187 \frac{\text{m}}{\text{s}^2}}$$

$$v_2 = v_1 + a \cdot t; \quad 6.94 = 0 + 0.0187 \cdot t$$

$$t = \frac{6.94}{0.0187} = \boxed{371 \text{ s}}$$

$$(17) \quad v_0 = 300 \frac{\text{km}}{\text{h}} = 83.3 \frac{\text{m}}{\text{s}}$$

a) $\hat{c} h_{\max}?$

b) $\hat{c} v?$

$$t = 3 \text{ s}$$

c) $\hat{c} t?$

$$a) \quad v^2 = v_0^2 - 2 \cdot g \cdot e$$

$$0 = 83.3^2 - 2 \cdot 10 \cdot e$$

$$0 = 6939 - 20 \cdot e$$

$$20 \cdot e = 6939$$

$$e = \frac{6939}{20} = \boxed{347 \text{ m}}$$

$$b) \quad v = v_0 - g \cdot t = 83.3 - 10 \cdot 3 = \boxed{53.3 \frac{\text{m}}{\text{s}}}$$

$$c) \quad v = v_0 - g \cdot t \Rightarrow 0 = 83.3 - 10 \cdot t \Rightarrow 10 \cdot t = 83.3 \Rightarrow$$

$$\Rightarrow t = \frac{83.3}{10} = \boxed{8.33 \text{ s}}$$

$$(18) \quad a) \quad t = 10 \text{ s}$$

$\hat{c} h?$

b) $\hat{c} t?$

$$v_0 = 80 \frac{\text{km}}{\text{h}} = 22.2 \frac{\text{m}}{\text{s}}$$

$$a) \quad e = \frac{1}{2} \cdot g \cdot t^2 =$$

$$= \frac{1}{2} \cdot 10 \cdot 10^2 = 5 \cdot 100 = \boxed{500 \text{ m}}$$

$$b) \quad e = v_0 \cdot t + \frac{1}{2} \cdot g \cdot t^2; \quad 500 = 22.2 \cdot t + \frac{1}{2} \cdot 10 \cdot t^2$$

$$5 \cdot t^2 + 22.2 \cdot t - 500 = 0$$

$$t = \frac{-22.2 \pm \sqrt{22.2^2 + 4 \cdot 5 \cdot 500}}{2 \cdot 5} = \boxed{8.02 \text{ s}}$$

19) $h_0 = 15 \text{ m}$

$v_0 = 12 \frac{\text{m}}{\text{s}}$

$\hat{c} h_{\text{max.}}?$

$\hat{c} t_T?$

$\hat{c} v?$

$$v^2 = v_0^2 - 2 \cdot g \cdot e_1$$

$$0 = 12^2 - 2 \cdot 10 \cdot e_1 ; 0 = 144 - 20 \cdot e_1 ;$$

$$20 \cdot e_1 = 144 ;$$

$$e_1 = \frac{144}{20} = 7.2 \text{ m}$$

$$h_{\text{max}} = h_0 + e_1 = 15 + 7.2 = \boxed{22.2 \text{ m}}$$

$$v = v_0 - g \cdot t_1 ; 0 = 12 - 10 \cdot t_1 ; 10 \cdot t_1 = 12 \Rightarrow t_1 = 1.2 \text{ s}$$

$$e = v_0 \cdot t + \frac{1}{2} \cdot g \cdot t^2 ; 22.2 = 0 + \frac{1}{2} \cdot 10 \cdot t_2^2 ;$$

$$22.2 = 5 \cdot t_2^2 ; t_2^2 = \frac{22.2}{5} = 4.44 ; t_2 = \sqrt{4.44} = \boxed{2.11 \text{ s}}$$

$$t_T = t_1 + t_2 = 1.2 + 2.11 = \boxed{3.31 \text{ s}}$$

$$v = v_0 + g \cdot t_2 = 0 + 10 \cdot 2.11 = \boxed{21.1 \frac{\text{m}}{\text{s}}}$$

20) $v_0 = 30 \frac{\text{m}}{\text{s}}$

a) $\hat{c} h, v?$

$t = 2 \text{ s}$

b) $\hat{c} h_{\text{max.}}?$

$\hat{c} t?$

c) $\hat{c} v?$

$h = 10 \text{ m}$

d) $\hat{c} v?$

$t = 5 \text{ s}$

a) $v^2 = v_0^2 - 2 \cdot g \cdot e ; v = v_0 - g \cdot t$

$$v = 30 - 10 \cdot 2 = \boxed{10 \frac{\text{m}}{\text{s}}}$$

$$e = v_0 \cdot t - \frac{1}{2} \cdot g \cdot t^2 = 30 \cdot 2 - \frac{1}{2} \cdot 10 \cdot 2^2 = 60 - 20 = \boxed{40 \text{ m}}$$

b) $v^2 = v_0^2 - 2 \cdot g \cdot e ; 0 = 30^2 - 2 \cdot 10 \cdot e \Rightarrow$
 $\Rightarrow 20 \cdot e = 900 \Rightarrow e = \frac{900}{20} = \boxed{45 \text{ m}}$

$v = v_0 - g \cdot t \Rightarrow 0 = 30 - 10 \cdot t \Rightarrow \boxed{t = 3 \text{ s}}$

c) $v^2 = v_0^2 - 2 \cdot g \cdot e = 30^2 - 2 \cdot 10 \cdot 10 \Rightarrow v = \boxed{26.5 \frac{\text{m}}{\text{s}}}$

d) $v = v_0 + g \cdot t = 0 + 10 \cdot 2 = \boxed{20 \frac{\text{m}}{\text{s}}}$

(21) $h_0 = 60 \text{ m}$ | $e = v_0 \cdot t + \frac{1}{2} \cdot g \cdot t^2 = 0 + \frac{1}{2} \cdot 10 \cdot 3^2 = \boxed{45 \text{ m}}$
 $\hat{h}, e?$ | $h = h_0 - e = 60 - 45 = \boxed{15 \text{ m}}$
 $t = 3 \text{ s}$ | $v = v_0 + g \cdot t = 0 + 10 \cdot 3 = \boxed{30 \frac{\text{m}}{\text{s}}}$
 $\hat{v}?$ | $e = v_0 \cdot t + \frac{1}{2} \cdot g \cdot t^2$
 $\hat{t}?$ | $60 = 0 + \frac{1}{2} \cdot 10 \cdot t^2 ; 60 = 5 \cdot t^2 ;$
 $\hat{v}?$

$$t^2 = \frac{60}{5} = 12 ; t = \sqrt{12} = \boxed{3.46 \text{ s}}$$

$$v = v_0 + g \cdot t = 0 + 10 \cdot 3.46 = \boxed{34.6 \frac{\text{m}}{\text{s}}}$$

(22) $h_0 = 10 \text{ m}$ | $v^2 = v_0^2 - 2 \cdot g \cdot e$
 $v_0 = 40 \frac{\text{km}}{\text{h}} = 11.1 \frac{\text{m}}{\text{s}}$ | $0 = 11.1^2 - 2 \cdot 10 \cdot e$
 $\hat{h}_{\text{max}}?$ | $0 = 123 - 20 \cdot e ; 20 \cdot e = 123$
 $\hat{v}?$ | $e = \frac{123}{20} = 6.15 \text{ m}$
 $\hat{t}_T?$ | $h_{\text{max}} = h_0 + e = 10 + 6.15 = \boxed{16.15 \text{ m}}$

$$v^2 = v_0^2 + 2 \cdot g \cdot e = 0 + 2 \cdot 10 \cdot 16.15 = 323 ; v = \sqrt{323} = \boxed{18 \frac{\text{m}}{\text{s}}}$$

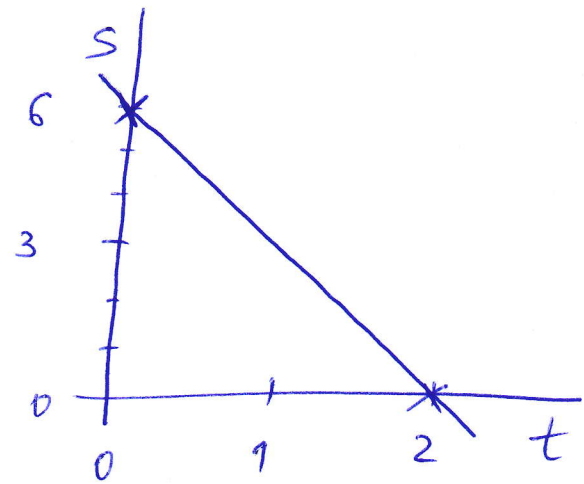
$$t_T = t_1 + t_2 ; v = v_0 - g \cdot t_1 = 11.1 - 10 \cdot t_1 \Rightarrow t_1 = 1.11 \text{ s}$$

$$v = v_0 + g \cdot t_2 \Rightarrow 18 = 0 + 10 \cdot t_2 \Rightarrow t_2 = 1.8 \text{ s}$$

$$t_T = t_1 + t_2 = 1.11 + 1.8 = \boxed{2.91 \text{ s}}$$

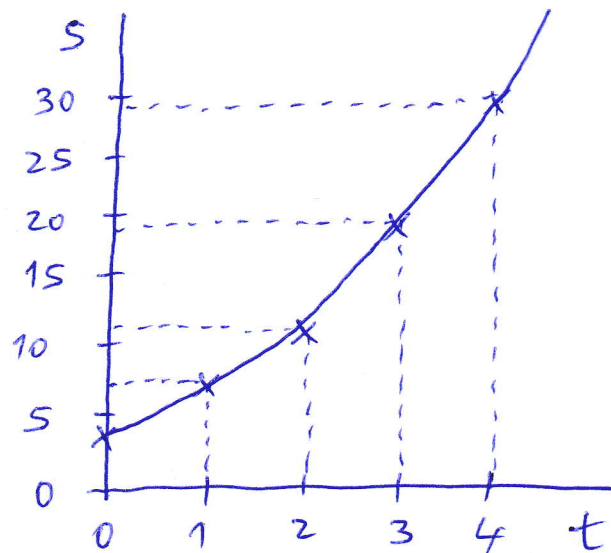
23

t	s
0	$-3 \cdot 0 + 6 = 6$
2	$-3 \cdot 2 + 6 = 0$



24

t	s
0	4
1	$1^2 + 2 \cdot 1 + 4 = 7$
2	$2^2 + 2 \cdot 2 + 4 = 12$
3	$3^2 + 2 \cdot 3 + 4 = 19$
4	$4^2 + 2 \cdot 4 + 4 = 28$



25

$$s = -m \cdot t + n$$

$$n = 30$$

$$m = \frac{\Delta s}{\Delta t} = \frac{30 - 20}{20 - 0} = \frac{10}{20} = 0.5$$

$$s = -0.5 \cdot t + 30$$

(26) * Primer método: cálculo gráfico de aceleraciones:

$$a_1 = \frac{\Delta v}{\Delta t} = \frac{15-5}{20-0} = \frac{10}{20} = 0'5 \frac{m}{s^2}$$

$$a_3 = \frac{\Delta v}{\Delta t} = \frac{25-15}{70-40} = \frac{10}{30} = 0'333 \frac{m}{s^2}$$

$$a_4 = \frac{\Delta v}{\Delta t} = \frac{25-0}{90-70} = \frac{25}{20} = 1'25 \frac{m}{s^2}$$

$$e_1 = v_0 \cdot t + \frac{1}{2} \cdot a_1 \cdot t^2 = 5 \cdot 20 + \frac{1}{2} \cdot 0'5 \cdot 20^2 = 200 \text{ m}$$

$$e_2 = v \cdot t = 15 \cdot 20 = 300 \text{ m}$$

$$e_3 = v_0 \cdot t + \frac{1}{2} \cdot a_3 \cdot t^2 = 15 \cdot 30 + \frac{1}{2} \cdot 0'333 \cdot 30^2 = 600 \text{ m}$$

$$e_4 = v_0 \cdot t - \frac{1}{2} \cdot a_4 \cdot t^2 = 25 \cdot 20 - \frac{1}{2} \cdot 1'25 \cdot 20^2 = 250 \text{ m}$$

$$e_T = 200 + 300 + 600 + 250 = \boxed{1350 \text{ m}}$$

* Segundo método: las áreas:

$$e_T = S_1 + S_2 + S_3 + S_4 + S_5 + S_6 =$$

$$= \frac{10 \cdot 20}{2} + 5 \cdot 20 + 15 \cdot 20 + \frac{10 \cdot 30}{2} + 15 \cdot 30 + \frac{25 \cdot 20}{2} =$$

$$= 100 + 100 + 300 + 150 + 450 + 250 =$$

$$= \boxed{1350 \text{ m}}$$

27) $D = 0'30 \text{ m}$

$\omega = 45 \text{ rpm}$

a) $\hat{d}\omega?$

b) $\hat{d}v?$

$R = 0'05 \text{ m}$

c) $\hat{d}v?$

d) $\hat{d}N?$

$t = 2 \text{ min } 47 \text{ s}$

e) $\hat{d}T?$

f) $\hat{d}f?$

a)

$$\omega = 45 \frac{\cancel{\text{rev}}}{\cancel{\text{min}}} \cdot \frac{2\pi \text{ rad}}{1 \cancel{\text{rev}}} \cdot \frac{1 \cancel{\text{min}}}{60 \text{ s}} =$$

$$= \boxed{4'71 \frac{\text{rad}}{\text{s}}}$$

b) $v = \omega \cdot R = 4'71 \cdot 0'05 = \boxed{0'236 \frac{\text{m}}{\text{s}}}$

c) $v = \omega \cdot R = 4'71 \cdot 0'15 = \boxed{0'706 \frac{\text{m}}{\text{s}}}$

d) $\varphi = \omega \cdot t = 4'71 \cdot 167 = 787 \text{ rad}$

$N = \frac{\varphi}{2\pi} = \frac{787}{2\pi} = \boxed{125 \text{ vueltas}}$

e) $T = \frac{2\pi}{\omega} = \frac{2\pi}{4'71} = \boxed{1'33 \text{ s}}$

$f = \frac{1}{T} = \frac{1}{1'33} = \boxed{0'752 \text{ Hz}}$

28) $R = 6370 \text{ km} = 6'37 \cdot 10^6 \text{ m}$

$\hat{d}\omega, v?$

$$\omega = \frac{\varphi}{T} = \frac{2\pi \text{ rad}}{24 \text{ h}} = \frac{2 \cdot \pi \text{ rad}}{24 \cdot 3600 \text{ s}} = \boxed{7'27 \cdot 10^{-5} \frac{\text{rad}}{\text{s}}}$$

$v = \omega \cdot R = 7'27 \cdot 10^{-5} \cdot 6'37 \cdot 10^6 = 463 \frac{\text{m}}{\text{s}} =$

$= 463 \cdot 3'6 = \boxed{1667 \frac{\text{km}}{\text{h}}}$

29) $D_1 = 1.8 \text{ m}$

$D_2 = 70 \text{ cm}$

$e = 100 \text{ m}$

$t = 2 \text{ min}$

$\omega_1, \omega_2?$

$v_1, v_2?$

$N_1, N_2?$

$$v = v_1 = v_2 = \frac{e}{t} = \frac{100}{2 \cdot 60} = \boxed{0.833 \frac{\text{m}}{\text{s}}}$$

$$v = \omega \cdot R \Rightarrow \omega = \frac{v}{R}$$

$$\omega_1 = \frac{v_1}{R_1} = \frac{0.833}{0.9} = \boxed{0.926 \frac{\text{rad}}{\text{s}}}$$

$$\omega_2 = \frac{v_2}{R_2} = \frac{0.833}{0.35} = \boxed{2.38 \frac{\text{rad}}{\text{s}}}$$

$$\varphi_1 = \omega_1 \cdot t = 0.926 \cdot 120 = 111 \text{ rad}$$

$$\varphi_2 = \omega_2 \cdot t = 2.38 \cdot 120 = 286 \text{ rad}$$

$$N_1 = \frac{\varphi_1}{2\pi} = \frac{111}{2\pi} = \boxed{17.7 \text{ vueltas}}$$

$$N_2 = \frac{\varphi_2}{2\pi} = \frac{286}{2\pi} = \boxed{45.5 \text{ vueltas}}$$

$$(30) \quad v = 50 \frac{\text{km}}{\text{h}} = 13.9 \frac{\text{m}}{\text{s}}$$

$$D = 0.70 \text{ m}$$

$$a) \text{ } \omega?$$

$$b) \text{ } N?$$

$$e = 20 \text{ km}$$

$$c) \text{ } e?$$

$$a) \quad v = \omega \cdot R$$

$$\omega = \frac{v}{R} = \frac{13.9}{0.35} = \boxed{39.7 \frac{\text{rad}}{\text{s}}}$$

$$b) \quad v = \frac{e}{t} \Rightarrow t = \frac{e}{v} = \frac{20000}{13.9} =$$

$$= 1439 \text{ s}$$

$$\varphi = \omega \cdot t = 39.7 \cdot 1439 = 5.71 \cdot 10^4 \text{ rad}$$

$$N = \frac{\varphi}{2\pi} = \frac{5.71 \cdot 10^4}{2 \cdot \pi} = \boxed{9088 \text{ vueltas}}$$

$$c) \quad e = \varphi \cdot R = 5.71 \cdot 10^4 \cdot 0.35 = \boxed{2 \cdot 10^4 \text{ m}}$$

$$(31) \quad \omega, T, f?$$

$$* \text{ Segundos: } T = 60 \text{ s} \quad f = \frac{1}{T} = \frac{1}{60} = \boxed{0.0167 \text{ Hz}}$$

$$\omega = \frac{2\pi}{T} = \frac{2 \cdot \pi}{60} = \boxed{0.105 \frac{\text{rad}}{\text{s}}}$$

$$* \text{ Minutos: } T = 1 \text{ h} = \boxed{3600 \text{ s}} \quad f = \frac{1}{T} = \frac{1}{3600} = \boxed{2.78 \cdot 10^{-4} \text{ Hz}}$$

$$\omega = \frac{2\pi}{T} = \frac{2 \cdot \pi}{\frac{2.78 \cdot 10^{-4}}{3600}} = \boxed{1.75 \cdot 10^{-3} \frac{\text{rad}}{\text{s}}}$$

$$* \text{ Horas: } T = 12 \text{ h} = 12 \cdot 3600 = \boxed{4.32 \cdot 10^4 \text{ s}}$$

$$f = \frac{1}{T} = \frac{1}{4.32 \cdot 10^4} = \boxed{2.31 \cdot 10^{-5} \text{ Hz}}$$

$$\omega = \frac{2\pi}{T} = \frac{2\pi}{4.32 \cdot 10^4} = \boxed{1.45 \cdot 10^{-4} \frac{\text{rad}}{\text{s}}}$$

32) $D_1 = 0.20 \text{ m}$

$D_2 = 0.15 \text{ m}$

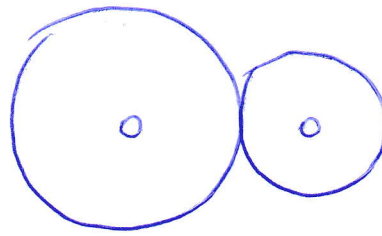
a) ω_2 ?

$N_1 = 50$

b) ω_2 ?

$\omega_1 = 40 \frac{\text{rad}}{\text{s}}$

b)



$v_1 = v_2 \Rightarrow \omega_1 \cdot R_1 = \omega_2 \cdot R_2$

$\omega_2 = \omega_1 \cdot \frac{R_1}{R_2} = 40 \cdot \frac{0.10}{0.075} = \boxed{53.3 \frac{\text{rad}}{\text{s}}}$

a) $N = \frac{\varphi}{2\pi}$; $\varphi = 2 \cdot \pi \cdot N$

$\varphi_1 = 2 \cdot \pi \cdot N_1 = 2 \cdot \pi \cdot 50 = 314 \text{ rad}$

$v_1 = v_2 \Rightarrow \omega_1 \cdot R_1 = \omega_2 \cdot R_2 \Rightarrow \frac{\varphi_1}{\cancel{2\pi}} \cdot R_1 = \frac{\varphi_2}{\cancel{2\pi}} \cdot R_2 \Rightarrow$

$\Rightarrow \cancel{2\pi} \cdot N_1 \cdot R_1 = \cancel{2\pi} \cdot N_2 \cdot R_2 \Rightarrow$

$\Rightarrow N_2 = N_1 \cdot \frac{R_1}{R_2} = 50 \cdot \frac{0.10}{0.075} = \boxed{66.7 \text{ vueltas}}$

33) $e = 200 \text{ m}$

$v_1 = 1/4 \frac{\text{m}}{\text{s}}$

$t = 2 \text{ min}$

$v_3 = 1/8 \frac{\text{m}}{\text{s}}$

a) $\hat{d} v_m$?

b) $\hat{d}$ desplazamiento?

c) $\hat{d} e$?

d) $\hat{d} v-t$?

e) $\hat{d} s-t$?

a) $v = \frac{e}{t} \Rightarrow t_1 = \frac{e}{v_1} = \frac{200}{1/4} = 143 \text{ s}$

$t_3 = \frac{e}{v_2} = \frac{200}{1/8} = 111 \text{ s}$

$v_m = \frac{e_T}{t_T} = \frac{e_1 + e_2 + e_3}{t_1 + t_2 + t_3} =$

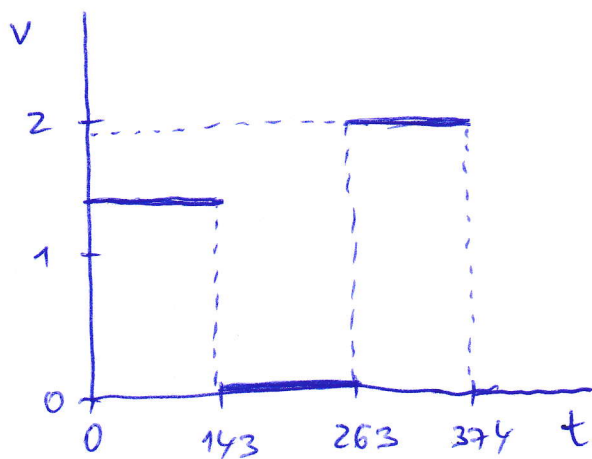
$= \frac{200 + 0 + 200}{143 + 120 + 111} = \frac{400}{374} = \boxed{1.07 \frac{\text{m}}{\text{s}}}$

b) Desplazamiento = $\boxed{0}$

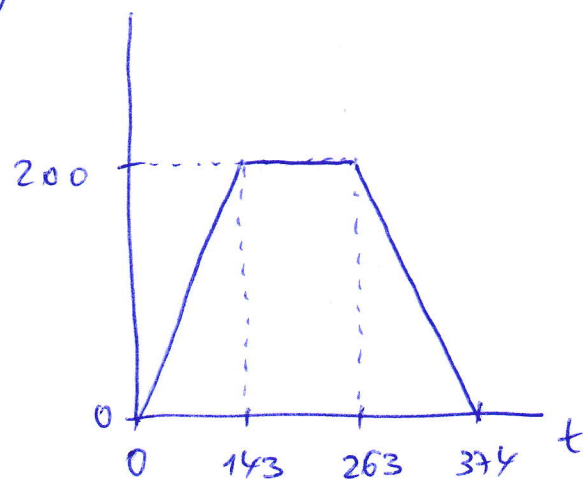
Es la distancia entre el punto inicial y el final.

c) $e = e_1 + e_2 + e_3 = 200 + 0 + 200 = \boxed{400 \text{ m}}$

d)



e)



$$(34) \quad v = 100 \frac{\text{km}}{\text{h}} = 27.8 \frac{\text{m}}{\text{s}}$$

$$d = 200 \text{ m}$$

$$t_R = 0.9 \text{ s}$$

$$a = 2 \frac{\text{m}}{\text{s}^2}$$

Hay dos tramos:

$$MAU + MAUR$$

$$e_T = e_1 + e_2$$

$$e_1 = v \cdot t = 27.8 \cdot 0.9 = 25 \text{ m}$$

$$x_{f/2} \quad v^2 = v_0^2 - 2 \cdot a \cdot e_2 \Rightarrow 0 = 27.8^2 - 2 \cdot 2 \cdot e_2 \Rightarrow$$

$$\Rightarrow 0 = 773 - 4 \cdot e_2 \Rightarrow 4 \cdot e_2 = 773 \Rightarrow e_2 = \frac{773}{4} = 193 \text{ m}$$

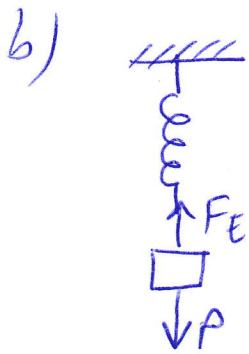
$$e_T = e_1 + e_2 = 25 + 193 = 218 \text{ m} > 200 \text{ m} \Rightarrow \boxed{\text{SÍ}}$$

Problemas resueltos de Dinámica

(11) a) $F_E = k \cdot x$

Para $F_E = 25 \text{ N}$, $x = 0.14 \text{ m} \Rightarrow$

$$\Rightarrow x = \frac{F_E}{k} = \frac{25}{179} = \boxed{179 \frac{\text{N}}{\text{m}}}$$



$$F_E = P \Rightarrow k \cdot x = m \cdot g \Rightarrow$$

$$\Rightarrow x = \frac{m \cdot g}{k} = \frac{0.2 \cdot 10}{179} =$$

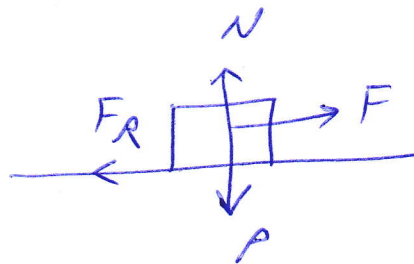
$$= 0.0112 \text{ m} = \boxed{1.12 \text{ cm}}$$

(12) $m = 50 \text{ kg}$

$$v = 20 \frac{\text{km}}{\text{h}} = 5.56 \frac{\text{m}}{\text{s}}$$

$\mu = ?$

$\mu = 0.4$



$$N = P$$

$$v = \text{cte} \Rightarrow F = F_R$$

$$F = F_R = \mu \cdot m \cdot g = 0.4 \cdot 50 \cdot 10 = \boxed{200 \text{ N}}$$

(13) $m = 70 \text{ kg}$

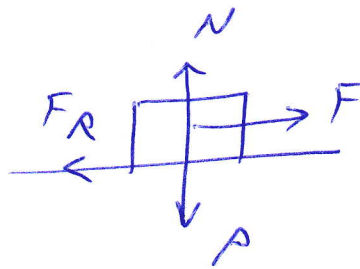
$v_0 = 0$

$v = 100 \frac{\text{km}}{\text{h}} = 27.8 \frac{\text{m}}{\text{s}}$

$t = 14 \text{ s}$

$\hat{=} F_0?$

$\mu = 0.3$



$F - F_R = m \cdot a$

$F_R = \mu \cdot m \cdot g = 0.3 \cdot 70 \cdot 10 = 210 \text{ N}$

$a = \frac{\Delta v}{\Delta t} = \frac{27.8 - 0}{14 - 0} = 1.99 \frac{\text{m}}{\text{s}^2}$

$F = F_R + m \cdot a = 210 + 70 \cdot 1.99 = \boxed{349 \text{ N}}$

(14) $m = 60 \text{ kg}$

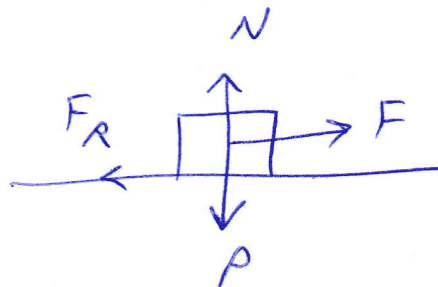
$\mu = 0.7$

$v_0 = 0$

$\hat{=} F_0?$

$e = 100 \text{ m}$

$t = 14 \text{ s}$



$F - F_R = m \cdot a$

$F_R = \mu \cdot m \cdot g = 0.7 \cdot 60 \cdot 10 = 420 \text{ N}$

$e = \frac{1}{2} \cdot a \cdot t^2$

$a = \frac{2 \cdot e}{t^2} = \frac{2 \cdot 100}{14^2} = 1.02 \frac{\text{m}}{\text{s}^2}$

$F = F_R + m \cdot a = 420 + 60 \cdot 1.02 = \boxed{481 \text{ N}}$

15) $m = 2000 \text{ kg}$

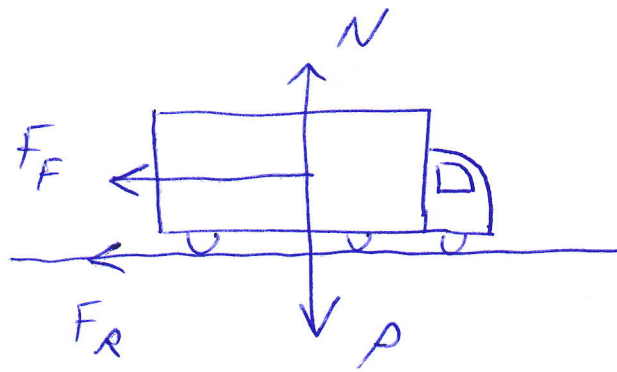
$v = 120 \frac{\text{km}}{\text{h}} = 33\frac{1}{3} \frac{\text{m}}{\text{s}}$

$\mu = 0.3$

$\hat{=} F_F?$

a) $t = 6 \text{ s}$

b) $e = 50 \text{ m}$



$F_F + F_R = m \cdot a$

a) $a = \frac{\Delta v}{\Delta t} = \frac{33\frac{1}{3} - 0}{6 - 0} = 5\frac{5}{6} \frac{\text{m}}{\text{s}^2}$

$F_R = \mu \cdot m \cdot g = 0.3 \cdot 2000 \cdot 10 = 6000 \text{ N}$

$F_F = m \cdot a - F_R = 2000 \cdot 5\frac{5}{6} - 6000 = \boxed{5100 \text{ N}}$

b) $v^2 = v_0^2 - 2 \cdot a \cdot e$

$0 = 33\frac{1}{3}^2 - 2 \cdot a \cdot 50 \Rightarrow 0 = 1109 - 100 \cdot a \Rightarrow$

$\Rightarrow 100 \cdot a = 1109 \Rightarrow a = \frac{1109}{100} = 11\frac{1}{10} \frac{\text{m}}{\text{s}^2}$

$F_F = m \cdot a - F_R = 2000 \cdot 11\frac{1}{10} - 6000 = \boxed{1.62 \cdot 10^4 \text{ N}}$

16) $m = 75 \text{ kg}$

$$v = 36 \frac{\text{km}}{\text{h}} = 10 \frac{\text{m}}{\text{s}}$$

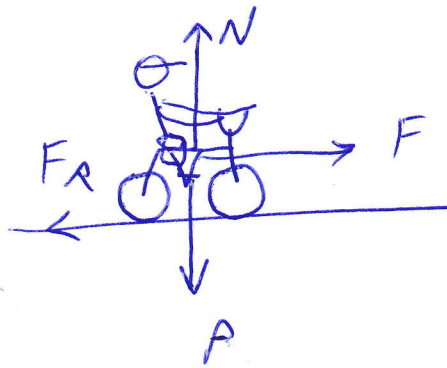
$$t = 60 \text{ s}$$

$$v_0 = 0$$

$$\mu = 0.08$$

a) $\vec{F}$?

b) $\vec{v}$?



a) $N = P$; $F - F_R = m \cdot a$

$$a = \frac{\Delta v}{\Delta t} = \frac{10 - 0}{60 - 0} = 0.167 \frac{\text{m}}{\text{s}^2}$$

$$F_R = \mu \cdot m \cdot g = 0.08 \cdot 75 \cdot 10 = 60 \text{ N}$$

$$F = F_R + m \cdot a = 60 + 75 \cdot 0.167 = \boxed{72.5 \text{ N}}$$

b) $R = F_R = 60 \text{ N} \Rightarrow a = \frac{R}{m} = \frac{60}{75} = 0.8 \frac{\text{m}}{\text{s}^2}$

$$v^2 = v_0^2 - 2 \cdot a \cdot e$$

$$0 = 10^2 - 2 \cdot 0.8 \cdot e ; \quad 0 = 100 - 1.6 \cdot e$$

$$1.6 \cdot e = 100 \Rightarrow e = \frac{100}{1.6} = \boxed{62.5 \text{ m}}$$

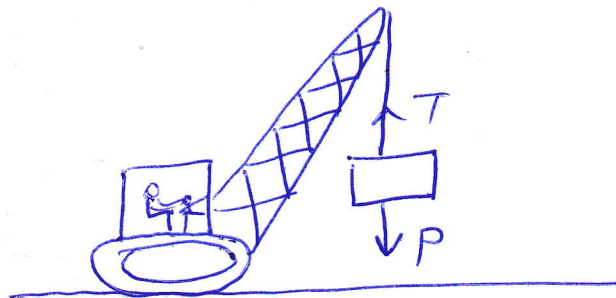
17) $m = 800 \text{ kg}$
 $\hat{P}?$

a) $v = 3 \frac{\text{m}}{\text{s}}$

b) $a = 0.5 \frac{\text{m}}{\text{s}^2}$

c) $\hat{t}?$

$e = 10 \text{ m}$



a) $v = cte \Rightarrow R = 0 \Rightarrow T = P =$
 $= m \cdot g = 800 \cdot 10 = \boxed{8000 \text{ N}}$

b) $a = cte \Rightarrow T - P = m \cdot a \Rightarrow$

$\Rightarrow T = P + m \cdot a = m \cdot g + m \cdot a = 800 \cdot 10 + 800 \cdot 0.5 = \boxed{8400 \text{ N}}$

c) * MRU: $v = \frac{e}{t} \Rightarrow t = \frac{e}{v} = \frac{10}{3} = \boxed{3.33 \text{ s}}$

* MRUA: $e = \frac{1}{2} \cdot a \cdot t^2$; $10 = \frac{1}{2} \cdot 0.5 \cdot t^2 \Rightarrow$

$\Rightarrow t^2 = \frac{2 \cdot 10}{0.5} = \frac{20}{0.5} = 40 \Rightarrow$

$\Rightarrow t = \sqrt{40} = \boxed{6.32 \text{ s}}$

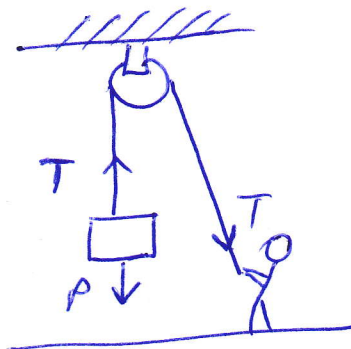
18) $m = 20 \text{ kg}$

a) $\vec{a}$ F?

$v = \text{cte}$

b) $\vec{a}$ F?

$a = 0,2 \frac{\text{m}}{\text{s}^2}$



a) $v = \text{cte} \Rightarrow R = 0 \Rightarrow$

$\Rightarrow T = P = m \cdot g = 20 \cdot 10 = \boxed{200 \text{ N}}$

b) $a = \text{cte} \Rightarrow T - P = m \cdot a \Rightarrow T = P + m \cdot a =$

$= m \cdot g + m \cdot a = 20 \cdot 10 + 20 \cdot 0,2 = \boxed{204 \text{ N}}$

19) $m_1 = 20 \text{ kg}$

$m_2 = 25 \text{ kg}$

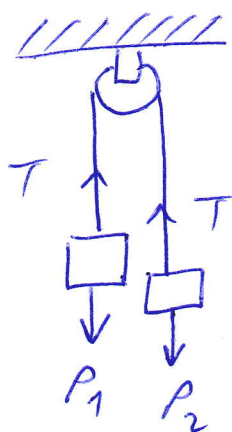
a) $\vec{a}$ f?

$h = 6 \text{ m}$

b) $\vec{a}$ T?

c) $\vec{a}$ f?

$e = 6 \text{ m}$



$P_1 = m_1 \cdot g = 200 \text{ N}$

$P_2 = m_2 \cdot g = 250 \text{ N}$

a) $P_2 - P_1 = m_T \cdot a$

$a = \frac{P_2 - P_1}{m_T} = \frac{250 - 200}{45} = 1,11 \frac{\text{m}}{\text{s}^2}$

$e = \frac{1}{2} \cdot a \cdot t^2 ; 6 = \frac{1}{2} \cdot 1,11 \cdot t^2 \Rightarrow t = \boxed{3,29 \text{ s}}$

b) $T - P_1 = m_1 \cdot a \Rightarrow T = P_1 + m_1 \cdot a = 200 + 20 \cdot 1,11 = \boxed{222 \text{ N}}$

c) Cada masa recorrería $3 \text{ m} \Rightarrow 3 = \frac{1}{2} \cdot 1,11 \cdot t^2 \Rightarrow \boxed{t = 2,33 \text{ s}}$
(6)

(20) $m = 80 \text{ kg}$

$\hat{?} F?$

$e = 10 \text{ m}$

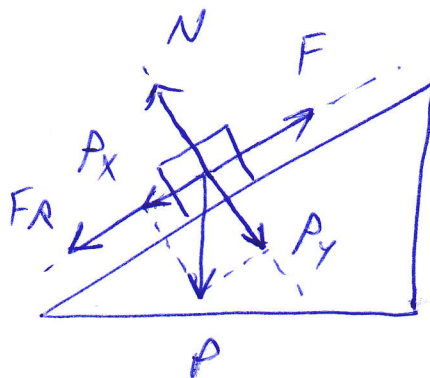
$t = 7 \text{ s}$

$v_0 = 0$

$\mu = 0.6$

$P_x = 514 \text{ N}$

$P_y = 613 \text{ N}$



$$R = m \cdot a \Rightarrow F - P_x - F_R = m \cdot a$$

$$F_R = \mu \cdot N = \mu \cdot P_y = 0.6 \cdot 613 = 368 \text{ N}$$

$$e = \frac{1}{2} \cdot a \cdot t^2; 10 = \frac{1}{2} \cdot a \cdot 7^2 \Rightarrow$$

$$\Rightarrow a = \frac{2 \cdot 10}{49} = 0.408 \frac{\text{m}}{\text{s}^2}$$

$$F = P_x + F_R + m \cdot a = 514 + 368 + 80 \cdot 0.408 = \boxed{915 \text{ N}}$$

(21) $\hat{?} F?$

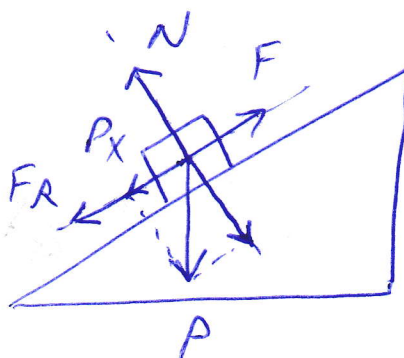
$m = 10 \text{ kg}$

$v = cte$

$\mu = 0.34$

$P_x = 766 \text{ N}$

$P_y = 643 \text{ N}$



$$v = cte \Rightarrow R = 0 \Rightarrow F = P_x + F_R$$

$$F_R = \mu \cdot N = \mu \cdot P_y = 0.34 \cdot 643 = 219 \text{ N}$$

$$F = P_x + F_R = 766 + 219 = \boxed{985 \text{ N}}$$

22) $m = 180 \text{ kg}$

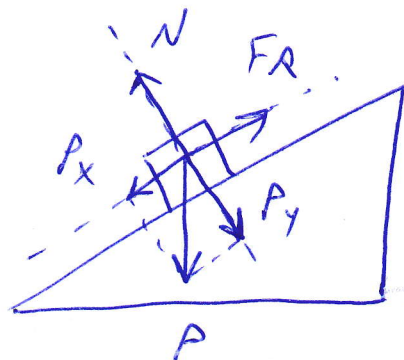
$e = 8 \text{ m}$

$P_x = 900 \text{ N}$

$P_y = 1559 \text{ N}$

at?

$\mu = 0.25$



$N = P_y$

$R = m \cdot a \Rightarrow P_x - F_R = m \cdot a$

$F_R = \mu \cdot N = 0.25 \cdot 1559 = 390 \text{ N}$

$a = \frac{P_x - F_R}{m} = \frac{900 - 390}{180} = 2.83 \frac{\text{m}}{\text{s}^2}$

$e = \frac{1}{2} \cdot a \cdot t^2 \Rightarrow 8 = \frac{1}{2} \cdot 2.83 \cdot t^2 \Rightarrow t^2 = \frac{2 \cdot 8}{2.83} = 5.65 \Rightarrow$

$\Rightarrow t = \sqrt{5.65} = \boxed{2.38 \text{ s}}$

23) at F?

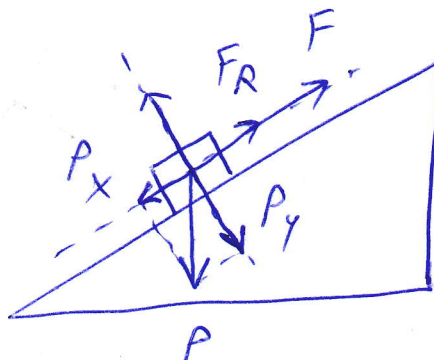
$m = 50 \text{ kg}$

$v = \text{cte}$

$\mu = 0.2$

$P_x = 321 \text{ N}$

$P_y = 383 \text{ N}$



$v = \text{cte} \Rightarrow R = 0 \Rightarrow P_x = F + F_R$

$F_R = \mu \cdot N = \mu \cdot P_y = 0.2 \cdot 383 = 76.6 \text{ N}$

$F = P_x - F_R = 321 - 76.6 = \boxed{244 \text{ N}}$

(24) $m = 70 \text{ kg}$

$F = 200 \text{ N}$

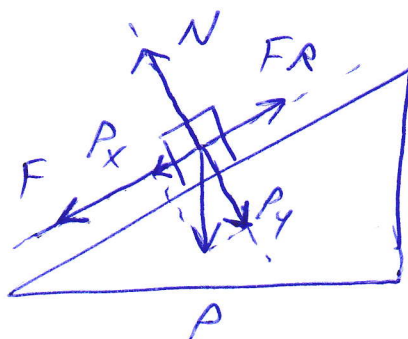
dit?

$e = 15 \text{ m}$

$P_x = 239 \text{ N}$

$P_y = 658 \text{ N}$

$\mu = 0.22$



$$F + P_x - F_R = m \cdot a$$

$$F_R = \mu \cdot N = \mu \cdot P_y = 0.22 \cdot 658 = 145 \text{ N}$$

$$a = \frac{F + P_x - F_R}{m} = \frac{200 + 239 - 145}{70} = 4.2 \frac{\text{m}}{\text{s}^2}$$

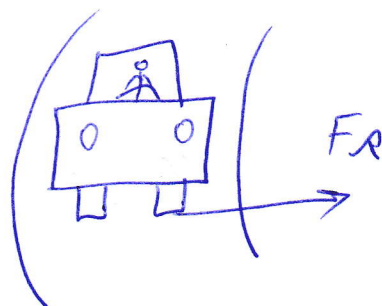
$$e = \frac{1}{2} \cdot a \cdot t^2 \Rightarrow 15 = \frac{1}{2} \cdot 4.2 \cdot t^2 \Rightarrow t^2 = \frac{15 \cdot 2}{4.2} = 7.14 \Rightarrow$$

$$\Rightarrow t = \sqrt{7.14} = \boxed{2.67 \text{ s}}$$

(25) $R = 40 \text{ m}$

dit?

$\mu = 0.6$



$$R = F_R = F_c \Rightarrow \mu \cdot m \cdot g = \frac{m \cdot v^2}{R} \Rightarrow$$

$$\Rightarrow v^2 = \mu \cdot g \cdot R \Rightarrow v = \sqrt{\mu \cdot g \cdot R} =$$

$$= \sqrt{0.6 \cdot 10 \cdot 40} = \sqrt{240} = \boxed{15.5 \frac{\text{m}}{\text{s}}}$$

(26) $m = 2000 \text{ kg}$

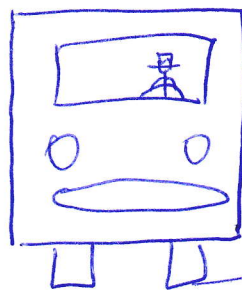
$v = 120 \frac{\text{km}}{\text{h}} = 33.3 \frac{\text{m}}{\text{s}}$

¿R?

$\mu = 0.4$

¿ a_n ?

¿ F_c ?



$F_R = F_c$

$R = F_R = F_c$

$\mu \cdot m \cdot g = \frac{m \cdot v^2}{R} \Rightarrow$

$\Rightarrow R = \frac{v^2}{\mu \cdot g} = \frac{33.3^2}{0.4 \cdot 10} = \boxed{277 \text{ m}}$

$a_n = \frac{v^2}{R} = \frac{33.3^2}{277} = \boxed{4 \frac{\text{m}}{\text{s}^2}}$

$F_c = m \cdot a_n = 2000 \cdot 4 = \boxed{8000 \text{ N}}$

(27) $v = 60 \frac{\text{km}}{\text{h}} = 16.7 \frac{\text{m}}{\text{s}}$

$R = 70 \text{ m}$

$\mu = 0.5$

$R = F_R = F_c$

$\mu \cdot m \cdot g = \frac{m \cdot v^2}{R}$

$v^2 = \mu \cdot g \cdot R$

$V_{\text{máx.}} = \sqrt{\mu \cdot g \cdot R} = \sqrt{0.5 \cdot 10 \cdot 70} = \sqrt{350} = 18.7 \frac{\text{m}}{\text{s}}$

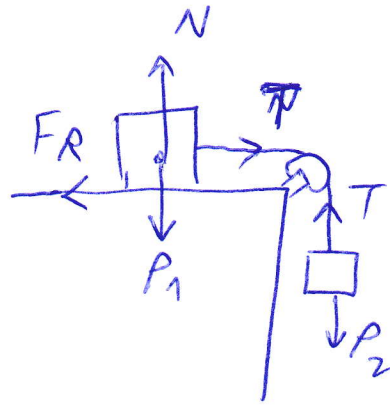
Al ser $16.7 \frac{\text{m}}{\text{s}}$ menor que la velocidad máxima permitida, no se saldrá.
(10)

28) $a?$

$$m_1 = 2 \text{ kg}$$

$$m_2 = 5 \text{ kg}$$

$$\mu = 0.35$$



$$R = m \cdot a \Rightarrow P_2 - F_R = m_T \cdot a$$

$$F_R = \mu \cdot P_1 = \mu \cdot m_1 \cdot g = 0.35 \cdot 2 \cdot 10 = 7 \text{ N}$$

$$a = \frac{P_2 - F_R}{m_T} = \frac{50 - 7}{7} = \frac{43}{7} = 6.14 \frac{\text{m}}{\text{s}^2}$$

PROBLEMAS RESUELTOS DE CÁLCULOS QUÍMICOS

1) $M = 2 \cdot 14 + 8 \cdot 1 + 2 \cdot 52 + 7 \cdot 16 = 252 \frac{\text{g}}{\text{mol}}$

a)

$$n = \frac{m}{M} = \frac{378}{252} = 1.5 \text{ mol}$$

b)

N:	$1.5 \cdot 2 = 3 \text{ mol}$
H:	$1.5 \cdot 8 = 12 \text{ mol}$
Cr:	$1.5 \cdot 2 = 3 \text{ mol}$
O:	$1.5 \cdot 7 = 10.5 \text{ mol}$

c)

N:	$3 \cdot 14 = 42 \text{ g}$
H:	$12 \cdot 1 = 12 \text{ g}$
Cr:	$3 \cdot 52 = 156 \text{ g}$
O:	$10.5 \cdot 16 = 168 \text{ g}$

d) $N = n \cdot N_A = 1.5 \cdot 6.022 \cdot 10^{23} = 9.03 \cdot 10^{23} \text{ moléculas}$

e)

N:	$3 \cdot 6.022 \cdot 10^{23} = 1.81 \cdot 10^{24} \text{ átomos}$
H:	$12 \cdot 6.022 \cdot 10^{23} = 7.23 \cdot 10^{24} \text{ ''}$
Cr:	$3 \cdot 6.022 \cdot 10^{23} = 1.81 \cdot 10^{24} \text{ ''}$
O:	$10.5 \cdot 6.022 \cdot 10^{23} = 6.32 \cdot 10^{24} \text{ ''}$

$$(2) \quad M = 2 \cdot 55.85 + 3 \cdot 16 = 159.7 \frac{\text{g}}{\text{mol}}$$

$$m_{\text{Fe}} = 150 \cancel{\text{g oligisto}} \cdot \frac{75 \cancel{\text{g Fe}_2\text{O}_3}}{100 \cancel{\text{g oligisto}}}$$

$$\cdot \frac{2 \cdot 55.85 \text{ g Fe}}{159.7 \cancel{\text{g Fe}_2\text{O}_3}} = \boxed{78.7 \text{ g Fe}}$$

$$(3) \quad m_{\text{N}_2} = 28 \frac{\text{g}}{\cancel{\text{mol}}} \cdot \frac{1 \cancel{\text{mol}}}{6.022 \cdot 10^{23} \text{ moléculas}} = \boxed{4.65 \cdot 10^{-23} \frac{\text{g}}{\text{molécula}}}$$

$$m_{\text{H}} = 1 \frac{\text{g}}{\cancel{\text{mol}}} \cdot \frac{1 \cancel{\text{mol}}}{6.022 \cdot 10^{23} \text{ átomos}} = \boxed{1.66 \cdot 10^{-24} \frac{\text{g}}{\text{átomo}}}$$

$$(4) \quad M = 4 \cdot 12 + 10 \cdot 1 + 16 = 74 \frac{\text{g}}{\text{mol}}$$

$$m = d \cdot V = 0.713 \frac{\text{g}}{\cancel{\text{cm}^3}} \cdot 250 \cancel{\text{cm}^3} = \boxed{178 \text{ g}}$$

$$n = \frac{m}{M} = \frac{178}{74} = \boxed{2.41 \text{ mol}}$$

$$N = n \cdot N_A = 2.41 \cdot 6.022 \cdot 10^{23} = \boxed{1.45 \cdot 10^{24} \text{ moléculas}}$$

$$\textcircled{5} \quad M = 2 \cdot 27 + 3 \cdot 16 = 102 \frac{\text{g}}{\text{mol}}$$

$$a) \quad n_{\text{Al}} = 1 \text{ ton mineral} \cdot \frac{10^6 \text{ g mineral}}{1 \text{ ton mineral}}$$

$$\cdot \frac{60 \text{ g Al}_2\text{O}_3}{100 \text{ g mineral}} \cdot \frac{1 \text{ mol Al}_2\text{O}_3}{102 \text{ g Al}_2\text{O}_3} \cdot \frac{2 \text{ mol Al}}{1 \text{ mol Al}_2\text{O}_3} =$$

$$= \boxed{1'18 \cdot 10^4 \text{ mol Al}}$$

$$b) \quad m = n \cdot M = 1'18 \cdot 10^4 \cdot 27 = \boxed{3'18 \cdot 10^5 \text{ g Al}}$$

$$c) \quad N = n \cdot N_A = 1'18 \cdot 10^4 \cdot 6'022 \cdot 10^{23} = \boxed{7'11 \cdot 10^{27} \text{ átomos Al}}$$

$$\textcircled{6} \quad M = 3 \cdot 55'85 + 2 \cdot 31 + 8 \cdot 16 = 357'6 \frac{\text{g}}{\text{mol}}$$

$$a) \quad n = \frac{m}{M} = \frac{80}{357'6} = \boxed{0'224 \text{ mol}}$$

$$b) \quad N = n \cdot N_A = 0'224 \cdot 6'022 \cdot 10^{23} = \boxed{1'35 \cdot 10^{23} \text{ moléculas}}$$

$$c) \quad \begin{array}{l} \text{Fe: } 0'224 \cdot 3 = \\ \text{P: } 0'224 \cdot 2 = \\ \text{O: } 0'224 \cdot 8 = \end{array} \boxed{\begin{array}{l} 0'672 \text{ mol} \\ 0'448 \text{ mol} \\ 1'79 \text{ mol} \end{array}}$$

$$d) \quad \begin{array}{l} \text{Fe: } 0'672 \cdot 55'85 = \\ \text{P: } 0'448 \cdot 31 = \\ \text{O: } 1'79 \cdot 16 = \end{array} \boxed{\begin{array}{l} 37'5 \text{ g} \\ 13'9 \text{ g} \\ 28'6 \text{ g} \end{array}}$$

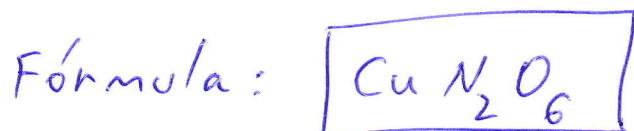
$$e) \quad \begin{array}{l} \text{Fe: } 0'672 \cdot 6'022 \cdot 10^{23} = \\ \text{P: } 0'448 \cdot 6'022 \cdot 10^{23} = \\ \text{O: } 1'79 \cdot 6'022 \cdot 10^{23} = \end{array} \boxed{\begin{array}{l} 4'05 \cdot 10^{23} \text{ átomos} \\ 2'70 \cdot 10^{23} \text{ ''} \\ 1'08 \cdot 10^{24} \text{ ''} \end{array}}$$

$$\textcircled{7} \quad m_0 = 1'07 - 0'36 - 0'16 = 0'55 \text{ g O}$$

$$\text{Cu: } \frac{0'36}{63'54} = 5'67 \cdot 10^{-3} \rightarrow \frac{5'67 \cdot 10^{-3}}{5'67 \cdot 10^{-3}} = 1$$

$$\text{N: } \frac{0'16}{14} = 0'0114 \rightarrow \frac{0'0114}{5'67 \cdot 10^{-3}} \approx 2$$

$$\text{O: } \frac{0'55}{16} = 0'0344 \rightarrow \frac{0'0344}{5'67 \cdot 10^{-3}} \approx 6$$

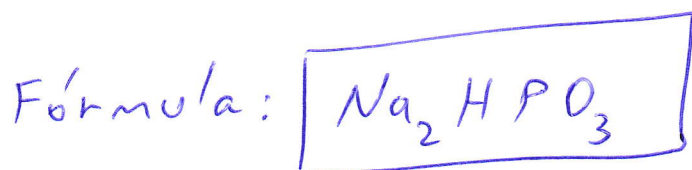


$$\textcircled{8} \quad \text{H: } \frac{0'8}{1} = 0'8 \rightarrow \frac{0'8}{0'793} \approx 1$$

$$\text{Na: } \frac{36'5}{23} = 1'58 \rightarrow \frac{1'58}{0'793} \approx 2$$

$$\text{P: } \frac{24'6}{31} = 0'793 \rightarrow \frac{0'793}{0'793} = 1$$

$$\text{O: } \frac{38'1}{16} = 2'38 \rightarrow \frac{2'38}{0'793} \approx 3$$



⑨ Fórmula semidesarrollada:



Fórmula molecular: $\text{C}_6\text{H}_{10}\text{O}_4\text{N}_2$

Fórmula empírica: $\text{C}_3\text{H}_5\text{O}_2\text{N}$

$$\textcircled{10} \text{ Sb: } \frac{25'4}{121'76} = 0'209 \rightarrow \frac{0'209}{0'209} = 1 \xrightarrow{\times 2} 2$$

$$\text{Se: } \frac{41'2}{78'96} = 0'522 \rightarrow \frac{0'522}{0'209} \approx 2'5 \xrightarrow{\times 2} 5$$

$$\text{O: } \frac{33'4}{16} = 2'09 \rightarrow \frac{2'09}{0'209} = 10 \xrightarrow{\times 2} 20$$

Fórmula: $\text{Sb}_2\text{Se}_5\text{O}_{20}$

$$\textcircled{11} M = 3 \cdot 112'41 + 2 \cdot 31 + 8 \cdot 16 = 527'2 \frac{\text{g}}{\text{mol}}$$

$$\text{Cd: } \frac{3 \cdot 112'41 \cdot 100}{527'2} = \boxed{64\%}$$

$$\text{P: } \frac{2 \cdot 31 \cdot 100}{527'2} = \boxed{11'8\%}$$

$$\text{O: } 100 - 64 - 11'8 = \boxed{24'2\%}$$

(6)

$$(12) \quad M = 2 \cdot 58'69 + 3 \cdot 12 + 9 \cdot 16 = 297'4 \frac{g}{mol}$$

$$Ni: \quad \frac{2 \cdot 58'69 \cdot 100}{297'4} = \boxed{39'5\%}$$

$$C: \quad \frac{3 \cdot 12 \cdot 100}{297'4} = \boxed{12'1\%}$$

$$O: \quad 100 - 39'5 - 12'1 = \boxed{48'4\%}$$

(13) Como no hay ningún dato de masa ni de volumen, hay que suponerlo:

$$40\% \rightarrow \begin{cases} 40 \text{ g HClO}_4 \\ 100 \text{ g disolución} \end{cases}$$

$$M = 1 + 35'5 + 16 \cdot 4 = 100'5 \frac{g}{mol}$$

$$n_s = \frac{m}{M} = \frac{40}{100'5} = 0'398 \text{ mol}; \quad V_D = \frac{m_D}{d_D} = \frac{100}{1'2} = 83'3 \text{ mL}$$

$$a) \quad c_M = \frac{n_s}{V_D} = \frac{0'398 \text{ mol}}{0'0833 \text{ L}} = \boxed{4'78 \text{ M}}$$

$$b) \quad c = \frac{m_s}{V_D} = \frac{40 \text{ g}}{0'0833 \text{ L}} = \boxed{480 \frac{g}{L}}$$

14) Como no hay ningún dato de masa ni de volumen, hay que suponerlo:

$$28\% \rightarrow \begin{cases} 28 \text{ g } \text{H}_2\text{SO}_4 \\ 100 \text{ g disolución} \end{cases}$$

$$M = 2 \cdot 1 + 32 + 4 \cdot 16 = 98 \frac{\text{g}}{\text{mol}}; n_s = \frac{m_s}{M_s} = \frac{28}{98} = 0.286 \text{ mol}$$

$$V_D = \frac{m_D}{d_D} = \frac{100}{1.25} = 80 \text{ mL} = 0.080 \text{ L}$$

$$a) c_M = \frac{n_s}{V_D} = \frac{0.286 \text{ mol}}{0.080 \text{ L}} = \boxed{3.57 \text{ M}}$$

$$b) c = \frac{m_s}{V_D} = \frac{28 \text{ g}}{0.080 \text{ L}} = \boxed{350 \frac{\text{g}}{\text{L}}}$$

15) a) $m_s = n_s \cdot M_s = 0.5 \cdot 98 = 49 \text{ g } \text{H}_2\text{SO}_4$

$$m_D = \frac{m_s \cdot 100}{\text{Perc.}} = \frac{49 \cdot 100}{53} = 92.4 \text{ g}$$

$$V_D = \frac{m_D}{d_D} = \frac{92.4 \text{ g}}{1.1 \text{ g/cm}^3} = \boxed{84 \text{ cm}^3}$$

$$b) m_D = d_D \cdot V_D = 1.1 \frac{\text{g}}{\text{cm}^3} \cdot 40 \text{ mL} = 44 \text{ g disolución}$$

$$m_s = \frac{\text{Perc.} \cdot m_D}{100} = \frac{53 \cdot 44}{100} = \boxed{23.3 \text{ g soluto}}$$

(8)

$$(16) \quad m_D = m_s + m_d = 40 + 80 = 120 \text{ g disolución}$$

$$V_D = \frac{m_D}{d_D} = \frac{120 \text{ g}}{1.12 \text{ g/mL}} = 107 \text{ mL} = 0.107 \text{ L}$$

$$V_d = \frac{m_d}{d_d} = \frac{80 \text{ g}}{1 \text{ g/mL}} = 80 \text{ mL}$$

$$V_s = V_D - V_d = 107 - 80 = 27 \text{ mL}$$

$$M_s = 23 + 35.5 = 58.5 \frac{\text{g}}{\text{mol}}$$

$$n_s = \frac{m_s}{M_s} = \frac{40 \text{ g}}{58.5 \frac{\text{g}}{\text{mol}}} = 0.684 \text{ mol}$$

* Porcentaje en masa:

$$\text{Porc. masa} = \frac{m_s \cdot 100}{m_D} = \frac{40 \cdot 100}{120} = \boxed{33.3\%}$$

* Masa por unidad de volumen:

$$c = \frac{m_s}{V_D} = \frac{40 \text{ g}}{0.107 \text{ L}} = \boxed{373 \frac{\text{g}}{\text{L}}}$$

* Porcentaje en volumen:

$$\text{Porc. volumen} = \frac{V_s \cdot 100}{V_D} = \frac{27 \cdot 100}{107} = \boxed{25.2\%}$$

* Molaridad:

$$c_M = \frac{n_s}{V_D} = \frac{0.684 \text{ mol}}{0.107 \text{ L}} = \boxed{6.38 \text{ M}}$$

(9)

17) Como no tenemos datos de masa ni de volumen, hay que suponerlo:

$$2 M \rightarrow \begin{cases} n_s = 2 \text{ mol } H_2SO_4 \\ V_D = 1 L \text{ disolución} \end{cases}$$

$$M_s = 2 \cdot 1 + 32 + 4 \cdot 16 = 98 \frac{g}{mol}$$

$$m_s = n_s \cdot M_s = 2 \text{ mol} \cdot 98 \frac{g}{\cancel{\text{mol}}} = 196 g$$

$$m_D = d_D \cdot V_D = 1 \frac{kg}{L} \cdot 1 L = 1 kg = 1000 g \text{ disolución}$$

* Porcentaje en masa:

$$\text{Porc. masa} = \frac{m_s \cdot 100}{m_D} = \frac{196 \cdot 100}{1000} = \boxed{19.6\%}$$

* Masa por unidad de volumen:

$$c = \frac{m_s}{V_D} = \frac{196 g}{1 L} = \boxed{196 \frac{g}{L}}$$

18) * Masa de disolución:

$$m_D = \frac{m_s \cdot 100}{\text{Porc.}} = \frac{50 \cdot 100}{60} = 83'3 \text{ g disolución}$$

* Volumen de disolución:

$$V_D = \frac{m_D}{d_D} = \frac{83'3 \text{ g}}{1'3 \frac{\text{g}}{\text{cm}^3}} = \boxed{64'1 \text{ cm}^3}$$

$1'3 \frac{\text{kg}}{\text{L}}$ es lo mismo que $1'3 \frac{\text{g}}{\text{cm}^3}$

19) * Número de moles del gas:

$$n = 0'175 \text{ L} \cdot \frac{1 \text{ mol}}{22'4 \text{ L}} = 7'81 \cdot 10^{-3} \text{ mol}$$

* Masa molecular del gas:

$$n = \frac{m}{M} \Rightarrow M = \frac{m}{n} = \frac{0'625 \text{ g}}{7'81 \cdot 10^{-3} \text{ mol}} = \boxed{80 \frac{\text{g}}{\text{mol}}}$$

$$20) \frac{P_1 \cdot V_1}{T_1} = \frac{P_2 \cdot V_2}{T_2}; T = \text{cte} \Rightarrow T_1 = T_2 \Rightarrow P_1 \cdot V_1 = P_2 \cdot V_2 \Rightarrow$$

$$\Rightarrow V_2 = \frac{P_1 \cdot V_1}{P_2} = \frac{1 \cdot 60}{5} = \boxed{12 \text{ L}}$$

$$(21) \quad P \cdot V = n \cdot R \cdot T \Rightarrow V = \frac{n \cdot R \cdot T}{P}$$

$$n = \frac{m}{M} = \frac{50}{32} = 1.56 \text{ mol} ; T_K = T_C + 273 = -30 + 273 = 243 \text{ K}$$

$$V = \frac{n \cdot R \cdot T}{P} = \frac{1.56 \cdot 0.082 \cdot 243}{2} = \boxed{15.6 \text{ L}}$$

$$(22) \quad \frac{P_1 \cdot V_1}{T_1} = \frac{P_2 \cdot V_2}{T_2} \Rightarrow V_2 = \frac{P_1 \cdot V_1 \cdot T_2}{P_2 \cdot T_1} =$$

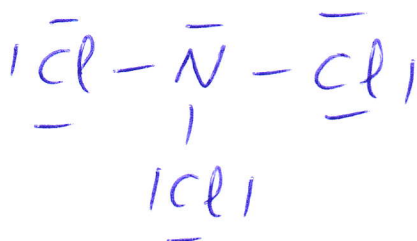
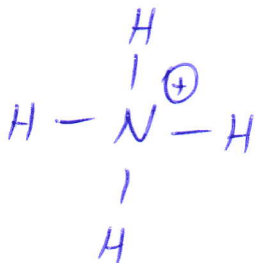
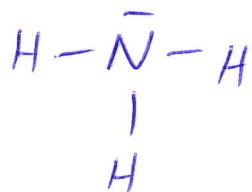
$$= \frac{3 \cdot 20 \cdot (273 + 40)}{1 \cdot (273 + 25)} = \frac{60 \cdot 313}{298} = \boxed{63 \text{ L}}$$

$$(23) \quad a)$$

$$1s^2 2s^2 2p^6 = [\text{He}] 2p^6$$

$$b) 1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} = [\text{Ar}] 4s^2 3d^{10}$$

$$c) 1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6 5s^2 4d^{10} 5p^6 6s^2 4f^{14} 5d^{10} 5p^6 7s^2 5f^{12} = [\text{Xe}] 7s^2 5f^{12}$$



$$(26) \quad T_K = T_C + 273 = 20 + 273 = 293 \text{ K}$$

$$P = \frac{300}{760} = 0.395 \text{ atm}$$

* Número de moles:

$$n = \frac{P \cdot V}{R \cdot T} = \frac{0.395 \cdot 5}{0.082 \cdot 293} = 0.822 \text{ mol } O_2$$

* Número de moléculas de O_2 :

$$N = n \cdot N_A = 0.822 \cdot 6.022 \cdot 10^{23} = 4.95 \cdot 10^{22} \text{ moléculas } O_2$$

* Número de átomos de O:

$$N = 4.95 \cdot 10^{22} \text{ moléculas } O_2 \cdot \frac{2 \text{ átomos O}}{1 \text{ molécula } O_2} =$$

$$= \boxed{9.9 \cdot 10^{22} \text{ átomos O}}$$

(27) * Número de moles del compuesto:

$$n = \frac{P \cdot V}{R \cdot T} = \frac{1'5 \cdot 40}{0'082 \cdot 293} = 2'5 \text{ mol}$$

* Masa molecular:

$$n = \frac{m}{M} \Rightarrow M_{\text{molecular}} = \frac{m}{n} = \frac{345 \text{ g}}{2'5 \text{ mol}} = 138 \frac{\text{g}}{\text{mol}}$$

* Masa de la fórmula empírica:

$$M_{\text{empírica}} = 2 \cdot 12 + 6 + 16 = 46 \frac{\text{g}}{\text{mol}}$$

* Coeficiente por el que hay que multiplicar la fórmula empírica:

$$x = \frac{M_{\text{molecular}}}{M_{\text{empírica}}} = \frac{138}{46} = 3$$

Fórmula molecular: $\boxed{\text{C}_6 \text{H}_{18} \text{O}_3}$

* Masas moleculares:

$$(28) \quad M_{\text{NaNO}_3} = 23 + 14 + 16 \cdot 3 = 85 \frac{\text{g}}{\text{mol}}$$

$$M_{\text{KNO}_3} = 39 + 14 + 16 \cdot 3 = 101 \frac{\text{g}}{\text{mol}}$$

* Porcentajes de N:

$$\text{En el NaNO}_3: \frac{14 \cdot 100}{85} = 16.5\%$$

$$\text{En el KNO}_3: \frac{14 \cdot 100}{101} = 13.8\%$$

Solución: NaNO_3